

§ 7-3 Conservation of Momentum

Recall Newton's Third Law:

$$\vec{F}_A = -\vec{F}_B$$

Recall $\vec{J} = \vec{F}\Delta t$
 $\vec{J} = \Delta\vec{p}$

$$\rightarrow \vec{F}_A \Delta t = -\vec{F}_B \Delta t$$

$$\Delta\vec{p}_A = -\Delta\vec{p}_B$$

(Think of object A's loss in momentum being equal to object B's gain in momentum)

$$\vec{p}'_A - \vec{p}_A = -(\vec{p}'_B - \vec{p}_B)$$

$$\vec{p}'_A - \vec{p}_A = -\vec{p}'_B + \vec{p}_B$$

$$\vec{p}'_A + \vec{p}'_B = \vec{p}_A + \vec{p}_B$$

Law of Conservation of Momentum

flip sides

$$\vec{p}_{\text{total}} = \vec{p}'_{\text{total}}$$

↑ obeyed in an isolated system (i.e. no friction)

* In PHY 11, we only deal with 1 dimensional collisions.

MP 313

	BEFORE		AFTER
	Car A	Car B	Car (A+B)
m	$1.75 \times 10^4 \text{ kg}$	$2.00 \times 10^4 \text{ kg}$	$3.75 \times 10^4 \text{ kg}$
v	+5.45 m/s	0	v
P	95375 kg·m/s	0	$(3.75 \times 10^4 \text{ kg})v$

Recall:
 $\vec{p} = m\vec{v}$

$\underbrace{\hspace{10em}}_{\vec{p}_{\text{total}}}$

 $\underbrace{\hspace{10em}}_{\vec{p}'_{\text{total}}}$

$$\vec{p}_A + \vec{p}_B = \vec{p}_{(A+B)}$$

$$\vec{p}_{\text{total}} = \vec{p}'_{\text{total}}$$

$$95375 \text{ kg}\cdot\text{m/s} = (3.75 \times 10^4 \text{ kg})v$$

$$v = +2.54 \text{ m/s}$$

$$\vec{v} = 2.54 \text{ m/s [EAST]}$$

Recoil of a Canoe

MP/316

	Before	After
	You+canoe	you canoe
M	180kg	65kg 115kg
V	0	+0.75m/s v
P	0	+48.75 kg·m/s (115kg)v
	\vec{P}_{total}	\vec{P}'_{total}

forward +

$$\vec{P}_{you+canoe} = \vec{P}_{you} + \vec{P}_{canoe}$$

$$m \cdot v$$

$$\vec{P}_{total} = \vec{P}'_{total}$$

$$0 = 48.75 \text{ kg} \cdot \text{m/s} + (115 \text{ kg})v$$

$$-48.75 \text{ kg} \cdot \text{m/s} = (115 \text{ kg})v$$

$$v = -0.42 \text{ m/s}$$

$$\vec{v} = 0.42 \text{ m/s [backward]}$$

To DO:

① PP/315

② PP/317